

Montogue

QUIZ MS203

Casting and Flow Stress

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PROBLEMS - CASTING

Problem 1

In the casting of steel under certain mold conditions, the mold constant in Chvorinov's rule is known to be 4.0 min/cm^2 , based on previous experience. The casting is a flat plate with length = 30 cm, width = 10 cm and thickness = 20 mm. Determine how long it will take for the casting to solidify.

- A) $t_s = 1.33 \text{ min.}$
- B) $t_s = 2.49 \text{ min.}$
- C) $t_s = 3.61 \text{ min.}$
- D) $t_s = 4.80 \text{ min.}$

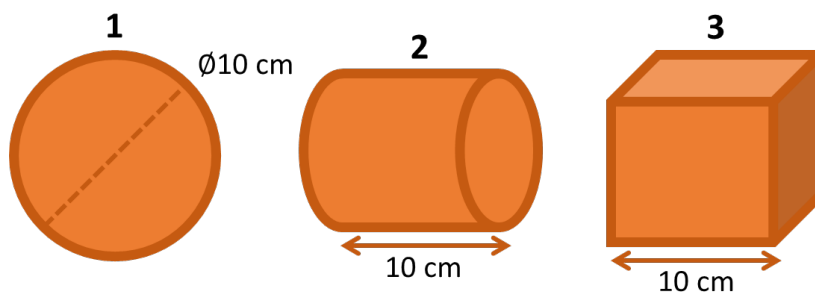
Problem 2

A rectangular casting having the dimensions 3 cm \times 5 cm \times 10 cm solidifies completely in 12 minutes. Compute the mold constant.

- A) $B = 10.1 \text{ min/cm}^2$
- B) $B = 14.5 \text{ min/cm}^2$
- C) $B = 19.3 \text{ min/cm}^2$
- D) $B = 22.2 \text{ min/cm}^2$

Problem 3 (Groover, 2013)

Total solidification times of three casting geometries are to be compared: (1) a sphere with diameter 10 cm; (2) a cylinder with diameter and length both 10 cm; and (3) a cube with side 10 cm. The same casting alloy is used in all three cases. Which geometry would completely solidify faster?



- A) The sphere.
- B) The cylinder.
- C) The cube.
- D) None of the above.

Problem 4 (Groover, 2013)

A riser in the shape of a sphere is to be designed for a sand casting mold. The casting is a rectangular plate with length = 200 mm, width = 100 mm, and thickness = 18 mm. If the total solidification time of the casting itself is known to be 3.5 min, determine the diameter of the riser so that it will take 25% longer for the riser to solidify.

- A) $D = 34.4 \text{ mm}$
- B) $D = 47.5 \text{ mm}$
- C) $D = 59.6 \text{ mm}$
- D) $D = 67.4 \text{ mm}$

Problem 5 (Groover, 2013)

A steel casting has a cylindrical geometry with 4.0 in. diameter and weighs 20 lb. The casting takes 6.0 min to completely solidify. Another cylindrical-shaped casting with the same diameter-to-length ratio weighs 12 lb. This casting is made of the same steel, and the same conditions of mold and pouring were used. The density of steel = 490 lb/ft³. True or false?

1. () The mold constant for either casting is greater than 10 min/in.²
2. () The lighter casting has diameter greater than 3.5 in. and length greater than 5 in.
3. () The solidification time for the lighter casting is greater than 5 minutes.

PROBLEMS - FLOW STRESS

Problem 6

The strength coefficient = 550 MPa and strain-hardening exponent = 0.22 for a certain metal. During a forming operation, the final true strain that the metal experiences = 0.85. Determine the flow stress at this strain and the average flow stress that the metal experienced during the operation.

- A) $\sigma_f = 531$ MPa and $\bar{\sigma}_f = 341$ MPa
- B) $\sigma_f = 531$ MPa and $\bar{\sigma}_f = 435$ MPa
- C) $\sigma_f = 572$ MPa and $\bar{\sigma}_f = 341$ MPa
- D) $\sigma_f = 572$ MPa and $\bar{\sigma}_f = 435$ MPa

Problem 7

A metal has a flow curve with strength coefficient = 850 MPa and strain-hardening exponent = 0.30. A tensile specimen of the metal with gage length = 100 mm is stretched to a length = 157 mm. Determine the flow stress at the new length and the average flow stress that the metal has been subjected to during the deformation.

- A) $\sigma_f = 669$ MPa and $\bar{\sigma}_f = 515$ MPa
- B) $\sigma_f = 669$ MPa and $\bar{\sigma}_f = 581$ MPa
- C) $\sigma_f = 731$ MPa and $\bar{\sigma}_f = 515$ MPa
- D) $\sigma_f = 731$ MPa and $\bar{\sigma}_f = 581$ MPa

Problem 8 (Creese, 1999)

The strength coefficient = 35,000 lb/in.² and strain-hardening exponent = 0.40 for a metal used in the forming operation in which the workpart is reduced in cross-sectional area by stretching. If the average flow stress on the part is 20,000 lb/in.², determine the amount of reduction in cross-sectional area experienced by the part. In the following answers, A_o and A_f denote initial and final cross-sectional area, respectively.

- A) $A_f = 0.331A_o$
- B) $A_f = 0.442A_o$
- C) $A_f = 0.565A_o$
- D) $A_f = 0.689A_o$

Problem 9 (Groover, 2013)

Determine the value of the strain-hardening exponent for a metal that will cause the average flow stress to be 3/4 of the final flow stress after deformation.

- A) $n = 0.143$
- B) $n = 0.215$
- C) $n = 0.333$
- D) $n = 0.416$

Problem 10 (Groover, 2013)

In a tensile test, two pairs of values of stress and strain were measured for the specimen metal after it had yielded: (1) true stress = 217 MPa and true strain = 0.35, and (2) true stress = 259 MPa and true strain = 0.68. Based on these data points, determine the strength coefficient and the strain-hardening exponent.

- A) $K = 201$ MPa and $n = 0.135$
- B) $K = 201$ MPa and $n = 0.271$
- C) $K = 290$ MPa and $n = 0.135$
- D) $K = 290$ MPa and $n = 0.271$

SOLUTIONS

P.1 ■ Solution

The volume of the casting is $V = 30 \times 10 \times 2 = 600 \text{ cm}^3$ and the surface area is $A = 2(30 \times 10 + 30 \times 2 + 10 \times 2) = 760 \text{ cm}^2$. Appealing to Chvorinov's rule, we obtain

$$t_s = B \left(\frac{V}{A} \right)^2 = 4.0 \times \left(\frac{600}{760} \right)^2 = \boxed{2.49 \text{ min}}$$

The casting should require about 2 and a half minutes to solidify.

- ◆ The correct answer is **B**.

P.2 ■ Solution

The surface area of the casting is $A = 2(3 \times 5 + 5 \times 10 + 3 \times 10) = 190 \text{ cm}^2$ and the volume is $V = 3 \times 5 \times 10 = 150 \text{ cm}^3$. The solidification time is 12 min. The mold constant can be established by substituting these data in Chvorinov's rule, namely

$$\begin{aligned} t_s &= B \left(\frac{V}{A} \right)^2 \rightarrow 12 = B \times \left(\frac{150}{190} \right)^2 \\ \therefore 12 &= B \times 0.623 \\ \therefore \boxed{B = 19.3 \text{ min/cm}^2} \end{aligned}$$

- ◆ The correct answer is **C**.

P.3 ■ Solution

For the sphere, the volume is $V_1 = \frac{4\pi R^3}{3} = 4\pi \times 5^3/3 = 524 \text{ cm}^3$ and the surface area is $A_1 = 4\pi R^2 = 4\pi \times 5^2 = 314 \text{ cm}^2$. The time required for solidification is calculated to be

$$\begin{aligned} t_{s,1} &= B \left(\frac{V_1}{A_1} \right)^n \rightarrow t_{s,1} = B \times \left(\frac{524}{314} \right)^2 \\ \therefore t_{s,1} &= 2.78B \end{aligned}$$

For the cylinder, the volume is $V_2 = \pi R^2 L = \pi \times 5^2 \times 10 = 785 \text{ cm}^3$ and the surface area is $A_2 = 2\pi R^2 + 2\pi RL = 2 \times \pi \times 5^2 + 2\pi \times 5 \times 10 = 471 \text{ cm}^2$. The time required for solidification is then

$$\begin{aligned} t_{s,2} &= B \left(\frac{V_2}{A_2} \right)^n \rightarrow t_{s,2} = B \times \left(\frac{785}{471} \right)^2 \\ \therefore t_{s,2} &= 2.78B \end{aligned}$$

For the cube, the volume is $V_3 = L^3 = 10^3 = 1000 \text{ cm}^3$ and the surface area is $A_3 = 6L^2 = 6 \times 10^2 = 600 \text{ cm}^2$. The time required for solidification follows as

$$\begin{aligned} t_{s,3} &= B \left(\frac{V_3}{A_3} \right)^n \rightarrow t_{s,3} = B \times \left(\frac{1000}{600} \right)^2 \\ \therefore t_{s,3} &= 2.78B \end{aligned}$$

Given that B is the same for all cases, we conclude that the solidification time will be approximately the same for all three geometries.

♦ The correct answer is **D**.

P.4 ■ Solution

The casting volume is $V = 200 \times 100 \times 18 = 360,000 \text{ mm}^3$ and the surface area is $A = 2(200 \times 100 + 200 \times 18 + 100 \times 18) = 50,800 \text{ mm}^2$. Given the solidification time $t_s = 3.5 \text{ min}$ for the casting, we can easily determine the mold constant,

$$t_s = B \left(\frac{V}{A} \right)^2 \rightarrow B = t_s \times \left(\frac{A}{V} \right)^2$$

$$\therefore B = 3.5 \times \left(\frac{50,800}{360,000} \right)^2 = 0.0697 \text{ min/mm}^2$$

Now, the riser volume is $V = \pi D^3/6 = 0.524D^3$ and the surface area $A = \pi D^2 = 3.14D^2$, so that $V/A = 0.524D^3/3.14D^2 = 0.167D$. Appealing to Chvorinov's rule again, we have

$$t_s = B \left(\frac{V}{A} \right)^2 \rightarrow 1.25 \times 3.5 = 0.0697 \times (0.167D)^2$$

$$\therefore 4.38 = 0.00194D^2$$

$$\therefore \boxed{D = 47.5 \text{ mm}}$$

♦ The correct answer is **B**.

P.5 ■ Solution

1.True. The density of steel is $\rho = 490/12^3 = 0.284 \text{ lb/in.}^3$. The volume of the casting follows as

$$\rho = \frac{m}{V} \rightarrow V = \frac{m}{\rho}$$

$$\therefore V = \frac{20}{0.284} = 70.4 \text{ in.}^3$$

Equipped with V , we can determine the length L of the casting,

$$V = \frac{\pi D^2 L}{4} \rightarrow L = \frac{4V}{\pi D^2}$$

$$\therefore L = \frac{4 \times 70.4}{\pi \times 4.0^2} = 5.60 \text{ in.}$$

The surface area is determined next,

$$A = \frac{2\pi D^2}{4} + \pi DL = \frac{2\pi \times 4.0^2}{4} + \pi \times 4.0 \times 5.60 = 95.5 \text{ in.}^2$$

We now have all the information necessary to determine the mold constant B ,

$$t_s = B \left(\frac{V}{A} \right)^2 \rightarrow B = t_s \times \left(\frac{A}{V} \right)^2$$

$$\therefore B = 6.0 \times \left(\frac{95.5}{70.4} \right)^2 = \boxed{11.0 \text{ min/in.}^2}$$

2.False. We first require the volume of the lighter casting. Since weight is proportional to volume, we can write

$$\frac{V_1}{W_1} = \frac{V_2}{W_2} \rightarrow V_2 = W_2 \times \frac{V_1}{W_1}$$

$$\therefore V_2 = 12 \times \frac{70.4}{20} = 42.2 \text{ in.}^3$$

We were told that the lighter casting has the same diameter-to-length ratio as the heavier one, namely

$$\frac{D_1}{L_1} = \frac{4.0}{5.60} = 0.714$$

This means that the relation $D_2 = 0.714L_2$, or, equivalently, $L_2 = 1.40D_2$ holds for the lighter casting. Thus,

$$V_2 = \frac{\pi D_2^2 L_2}{4} \rightarrow V_2 = \frac{\pi D_2^2 \times 1.40D_2}{4}$$

$$\therefore V_2 = 0.35\pi D_2^3$$

$$\therefore D_2 = \left(\frac{V_2}{0.35\pi} \right)^{\frac{1}{3}}$$

$$\therefore D_2 = \left(\frac{42.2}{0.35\pi} \right)^{\frac{1}{3}} = \boxed{3.37 \text{ in.}}$$

Finally,

$$L_2 = 1.40D_2 = 1.40 \times 3.37 = \boxed{4.72 \text{ in.}}$$

3.False. From Part 2, we know that the volume of the lighter casting is $V_2 = 42.2 \text{ in.}^3$. The surface area is calculated as

$$A_2 = \frac{2\pi D_2^2}{4} + \pi D_2 L_2 = \frac{2\pi \times 3.37^2}{4} + \pi \times 3.37 \times 4.72 = 67.8 \text{ in.}^2$$

Lastly, the solidification time is determined to be

$$t_{s,2} = B \left(\frac{V_2}{A_2} \right)^2 = 11.0 \times \left(\frac{42.2}{67.8} \right)^2 = \boxed{4.26 \text{ min}}$$

P.6 ■ Solution

The flow stress is simply

$$\sigma_f = K \varepsilon^n = 550 \times 0.85^{0.22} = \boxed{531 \text{ MPa}}$$

The average flow stress is, in turn,

$$\bar{\sigma}_f = \frac{K \varepsilon^n}{n+1} = \frac{550 \times 0.85^{0.22}}{1.22} = \boxed{435 \text{ MPa}}$$

◆ The correct answer is **B**.

P.7 ■ Solution

The true strain in the specimen is

$$\varepsilon = \ln(157/100) = 0.451$$

The flow stress is then

$$\sigma_f = K \varepsilon^n = 850 \times 0.451^{0.30} = \boxed{669 \text{ MPa}}$$

while the average flow stress is calculated as

$$\bar{\sigma}_f = \frac{K \varepsilon^n}{n+1} = \frac{850 \times 0.451^{0.30}}{0.30+1} = \boxed{515 \text{ MPa}}$$

◆ The correct answer is **A**.

P.8 ■ Solution

With recourse to the equation for average flow stress, we write

$$\bar{\sigma}_f = \frac{K \varepsilon^n}{n+1} \rightarrow 20,000 = \frac{35,000 \times \varepsilon^{0.40}}{0.40+1}$$

$$\therefore \varepsilon = 0.572$$

Since $\varepsilon = \ln(A_o/A_f)$, it follows that

$$\begin{aligned}\varepsilon &= \ln\left(\frac{A_o}{A_f}\right) \rightarrow 0.572 = \ln\left(\frac{A_o}{A_f}\right) \\ \therefore A_o/A_f &= 1.77 \\ \therefore \boxed{A_f = 0.565A_o}\end{aligned}$$

◆ The correct answer is **C**.

P.9 ■ Solution

In accordance with the problem statement, we must have $\bar{\sigma}_f = 0.75\sigma_f$. Therefore,

$$\begin{aligned}\bar{\sigma}_f = 0.75\sigma_f &\rightarrow \frac{K\varepsilon^n}{n+1} = 0.75 \times K\varepsilon^n \\ \therefore \frac{1}{n+1} &= 0.75 \\ \therefore 1 &= 0.75n + 0.75 \\ \therefore n &= \frac{0.25}{0.75} = \boxed{0.333}\end{aligned}$$

◆ The correct answer is **C**.

P.10 ■ Solution

Using logarithms, the flow stress equation can be adjusted as

$$\begin{aligned}\sigma_f = K\varepsilon^n &\rightarrow \ln \sigma_f = \ln(K\varepsilon^n) \\ \therefore \ln \sigma_f &= \ln K + \ln \varepsilon^n \\ \therefore \ln \sigma_f &= \ln K + n \ln \varepsilon\end{aligned}$$

Substituting the first data point, we have

$$\begin{aligned}\ln 217 &= \ln K + n \ln 0.35 \\ \therefore 5.38 &= \ln K - 1.05n \quad (\text{I})\end{aligned}$$

Substituting the second data point, we have

$$\begin{aligned}\ln 259 &= \ln K + n \ln 0.68 \\ \therefore 5.56 &= \ln K - 0.386n \quad (\text{II})\end{aligned}$$

Subtracting equation (II) from (I) brings to

$$\begin{aligned}5.38 - 5.56 &= \ln K - 1.05n - (\ln K - 0.386n) \\ \therefore -0.18 &= -0.664n \\ \therefore \boxed{n = 0.271}\end{aligned}$$

Inserting this result into equation (I) yields

$$\begin{aligned}5.38 &= \ln K - 1.05 \times 0.271 \\ \therefore 5.38 &= \ln K - 0.285 \\ \therefore \ln K &= 5.67 \\ \therefore K &= e^{5.67} = \boxed{290 \text{ MPa}}\end{aligned}$$

◆ The correct answer is **D**.

ANSWER SUMMARY

Problem 1	B
Problem 2	C
Problem 3	D
Problem 4	B
Problem 5	T/F
Problem 6	B
Problem 7	A
Problem 8	C
Problem 9	C
Problem 10	D

REFERENCES

- CREESE, R. (1999). *Introduction to Manufacturing Processes and Materials*. New York: Marcel Dekker.
- GROOVER, M. (2013). *Fundamentals of Modern Manufacturing*. 5th edition. Hoboken: John Wiley and Sons.



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